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Research and Statistical Support University of North Texas

Identifying or Verifying the Number of Factors to Extract u Very Simple Structure.

Link to the last RSS article here: [Statistical Resources \(update: version 3\)](#). -- Ed.

By [Dr. Jon Starkweather](#), Research and Statistical Support Consultant Team

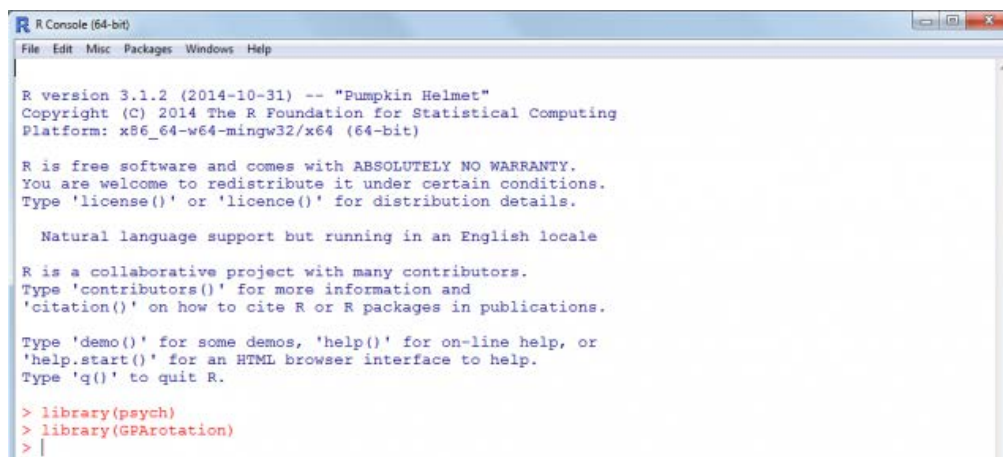
Factor analysis is perhaps one of the most frequently used analyses. It is versatile and flexible; meaning, it can be applied to a variety of data situations and types, and it can be applied in a variety of ways. However, conducting factor analysis generally requires the data analyst to make several decisions. Analysts often run several factor analyses, even when attempting to *confirm* an established factor structure; in order to assess the fit of the data to several factor models (e.g. one factor model, two factor model, three factor model, etc.). Over the 100 years since Spearman (1904) developed factor analysis there have been many, many criteria proposed for determining the number of factors to extract (e.g. eigenvalues greater than one, Horn's [1965] parallel analysis, Cattell's [1966] scree plot or test, Velicer's [1976] Minimum Average Partial [MAP] criterion, etc.). Each of these proposed criteria have strengths and weaknesses; and they occasionally conflict with one another, which makes using one criterion over another a risky proposition. This month's article demonstrates a very handy method for comparing multiple criteria in the pursuit of choosing to extract the appropriate number of factors during factor analysis.

In popular culture it is not uncommon to hear someone say, "There's an *app* for that." The phrase generally refers to the idea that an *application* exists (for a smart phone) which does the task being discussed. Likewise, here at RSS we very frequently find "There's a *pack* for that." This phrase refers to the virtual certainty of finding an R *package* which has a function devoted to some analysis or technique we are discussing. The primary package we will be using here is one package which contains a great many useful functions and as a result is very often *the* package we end up using for a variety of analyses. The primary package we will be using here is the 'psych' package (Revelle, 2014). The 'psych' package has grown substantially over the last few years and includes many very useful functions – if you have not taken a look at it recently, you might want to check it out.

Our examples below will actually require two packages, the 'psych' package and the 'GPArotation' package (Bernaards & Jennrich, 2014). The 'GPArotation' package should be familiar to anyone with experience doing factor analysis – it provides functions for several rotation strategies. The primary function we demonstrate below is the 'vss' function from the 'psych' package. The *Very Simple Structure* (VSS; Revell & Rocklin, 1979) function provides a nice output of criteria for varying levels of factor model complexity (i.e. number of factors to extract). The Very Simple Structure (VSS) terminology is used to refer to the idea that all loadings which are less than the maximum loading (of an item to a factor) are suppressed to zero – thus forcing a particular factor model to be much more interpretable or more clearly distinguished. Then, fit of several models of increasing rank complexity (i.e. more and more factors specified) can be assessed using the residual matrix of each model (i.e. original matrix minus the reproduced matrix of the models). We will also be using both the 'fa' function (from the 'psych' package) and the 'factanal' function (from the 'stats' package – included with all installations of R) to fit factor analysis models to the data structures.

Examples

The first two examples used here can easily be duplicated using the scripts provided below (i.e. the data file is available at the URL in the script / screen capture image). The third example is the example contained in the help file of the 'vss' function and can be accessed using the script below. First, load the two packages we will be using.



```
R Console (64-bit)
File Edit Misc Packages Windows Help

R version 3.1.2 (2014-10-31) -- "Pumpkin Helmet"
Copyright (C) 2014 The R Foundation for Statistical Computing
Platform: x86_64-w64-mingw32/x64 (64-bit)

R is free software and comes with ABSOLUTELY NO WARRANTY.
You are welcome to redistribute it under certain conditions.
Type 'license()' or 'licence()' for distribution details.

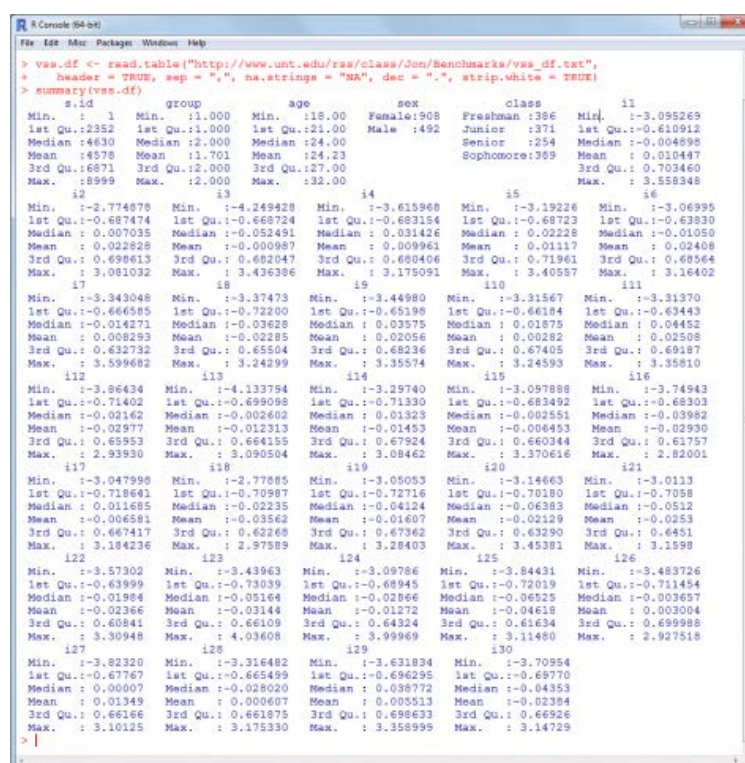
Natural language support but running in an English locale

R is a collaborative project with many contributors.
Type 'contributors()' for more information and
'citation()' on how to cite R or R packages in publications.

Type 'demo()' for some demos, 'help()' for on-line help, or
'help.start()' for an HTML browser interface to help.
Type 'q()' to quit R.

> library(psych)
> library(GPArotation)
> |
```

Next, we will import the comma delimited text (.txt) file from the RSS server using the URL and file name (vss_df.txt) contained in the script / image below. We also run a simple 'summary' on the data frame to make sure it was imported correctly.



```
R Console (64-bit)
File Edit Misc Packages Windows Help

> vss_df <- read.table("http://www.unt.edu/rss/class/Jon/benchmarks/vss_df.txt",
+ header = TRUE, sep = ",", na.strings = "NA", dec = ".", strip.white = TRUE)
> summary(vss_df)
  s.id      group      age      sex      class      il
Min.   : 1      Min.  :1.000      Min.  :18.00      Female:908      Freshman:386      Min.   :-3.095269
1st Qu.:2252      1st Qu.:1.000      1st Qu.:21.00      Male:492        Junior:371        1st Qu.:-0.610912
Median :4630      Median :2.000      Median :24.00                                Senior:254        Median :-0.004898
Mean   :4578      Mean   :1.701      Mean   :24.23                                Sophomore:359     Mean   :-0.010447
3rd Qu.:16871     3rd Qu.:12.000     3rd Qu.:127.00                                3rd Qu.: 0.703460
Max.   :8999      Max.   :2.000      Max.   :32.00                                Max.   : 3.558348

  i2      i3      i4      i5      i6
Min.   :-2.774878      Min.   :-4.249428      Min.   :-3.615968      Min.   :-3.19226      Min.   :-3.06995
1st Qu.:-0.687474      1st Qu.:-0.668724      1st Qu.:-0.683154      1st Qu.:-0.68723      1st Qu.:-0.63830
Median : 0.007035      Median :-0.052491      Median : 0.031426      Median : 0.02228      Median :-0.01050
Mean   : 0.022828      Mean   :-0.000987      Mean   : 0.009961      Mean   : 0.01117      Mean   : 0.02408
3rd Qu.: 0.698613      3rd Qu.: 0.682047      3rd Qu.: 0.680406      3rd Qu.: 0.71961      3rd Qu.: 0.68564
Max.   : 3.081032      Max.   : 3.436386      Max.   : 3.175091      Max.   : 3.40557      Max.   : 3.16402

  i7      i8      i9      i10     i11
Min.   :-3.343048      Min.   :-3.37473      Min.   :-3.44980      Min.   :-3.31567      Min.   :-3.31370
1st Qu.:-0.666585      1st Qu.:-0.72200      1st Qu.:-0.65198      1st Qu.:-0.66184      1st Qu.:-0.63443
Median :-0.014271      Median :-0.03628      Median : 0.03575      Median : 0.01875      Median : 0.04452
Mean   : 0.008293      Mean   :-0.02285      Mean   : 0.02056      Mean   : 0.00282      Mean   : 0.02508
3rd Qu.: 0.632732      3rd Qu.: 0.65504      3rd Qu.: 0.68236      3rd Qu.: 0.67405      3rd Qu.: 0.60187
Max.   : 3.599682      Max.   : 3.24299      Max.   : 3.35574      Max.   : 3.24593      Max.   : 3.35810

  i12     i13     i14     i15     i16
Min.   :-3.86434      Min.   :-4.133794      Min.   :-3.29740      Min.   :-3.09788      Min.   :-3.74943
1st Qu.:-0.71402      1st Qu.:-0.699098      1st Qu.:-0.71330      1st Qu.:-0.683492      1st Qu.:-0.68303
Median :-0.02142      Median :-0.002602      Median : 0.01323      Median :-0.002551      Median :-0.03982
Mean   :-0.02977      Mean   :-0.012313      Mean   :-0.01453      Mean   :-0.006453      Mean   :-0.02930
3rd Qu.: 0.65853      3rd Qu.: 0.664155      3rd Qu.: 0.67924      3rd Qu.: 0.660344      3rd Qu.: 0.61757
Max.   : 2.93930      Max.   : 3.090504      Max.   : 3.08462      Max.   : 3.370616      Max.   : 2.82001

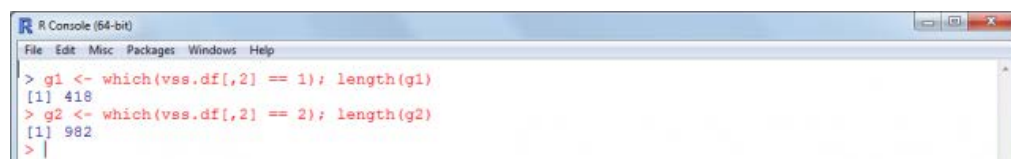
  i17     i18     i19     i20     i21
Min.   :-3.047998      Min.   :-2.77885      Min.   :-3.05053      Min.   :-3.14663      Min.   :-3.0113
1st Qu.:-0.718641      1st Qu.:-0.70987      1st Qu.:-0.72716      1st Qu.:-0.70280      1st Qu.:-0.7058
Median : 0.011685      Median :-0.02235      Median :-0.04124      Median :-0.06383      Median :-0.0512
Mean   :-0.006581      Mean   :-0.03562      Mean   :-0.01607      Mean   :-0.02129      Mean   :-0.0253
3rd Qu.: 0.667417      3rd Qu.: 0.62268      3rd Qu.: 0.67362      3rd Qu.: 0.63290      3rd Qu.: 0.6451
Max.   : 3.184236      Max.   : 2.97589      Max.   : 3.28403      Max.   : 3.45381      Max.   : 3.1598

  i22     i23     i24     i25     i26
Min.   :-3.57302      Min.   :-3.43963      Min.   :-3.09786      Min.   :-3.84431      Min.   :-3.483726
1st Qu.:-0.63999      1st Qu.:-0.73039      1st Qu.:-0.68945      1st Qu.:-0.72019      1st Qu.:-0.711454
Median :-0.01984      Median :-0.05164      Median :-0.02866      Median :-0.06525      Median :-0.003657
Mean   :-0.02366      Mean   :-0.03144      Mean   :-0.01272      Mean   :-0.04618      Mean   : 0.003004
3rd Qu.: 0.60841      3rd Qu.: 0.66109      3rd Qu.: 0.64324      3rd Qu.: 0.61634      3rd Qu.: 0.699988
Max.   : 3.30948      Max.   : 4.03608      Max.   : 3.99869      Max.   : 3.11460      Max.   : 2.927518

  i27     i28     i29     i30
Min.   :-3.82320      Min.   :-3.316482      Min.   :-3.631834      Min.   :-3.70954
1st Qu.:-0.67767      1st Qu.:-0.665499      1st Qu.:-0.696295      1st Qu.:-0.69770
Median : 0.00007      Median :-0.028020      Median : 0.038772      Median :-0.04353
Mean   : 0.01349      Mean   : 0.000607      Mean   : 0.005513      Mean   :-0.02384
3rd Qu.: 0.66166      3rd Qu.: 0.661875      3rd Qu.: 0.698633      3rd Qu.: 0.66926
Max.   : 3.10125      Max.   : 3.175330      Max.   : 3.358995      Max.   : 3.14729

> |
```

The simulated data includes a sample identification number for each participant (s.id), a grouping variable (group 1 or group 2), age of each participant (age in years), sex of each participant (female or male), class standing of each participant (freshman, sophomore, junior, or senior), and 30 item scores. Next, we will identify which participants belong to group 1 and which belong to group 2; as well as the number of participants in each group.



```
R Console (64-bit)
File Edit Misc Packages Windows Help

> g1 <- which(vss_df[,2] == 1); length(g1)
[1] 418
> g2 <- which(vss_df[,2] == 2); length(g2)
[1] 982
> |
```

So, we have 418 participants in group 1 and 982 participants in group 2. Generally when analysts intend to do factor analysis they have an idea of how many factors they believe the appropriate factor model contains; and often they have an idea of whether an orthogonal or oblique rotation strategy is warranted. For this first example (i.e. group 1) looking at the 30 item scores (i.e. columns 6 through 35), we believe there are two factors and therefore; we specify 3 factors ($n = 3$) in the 'vss' function. We also believe the factors are likely to be meaningfully related and

consequently, we specify an oblimin rotation strategy. Next, we apply the 'vss' function to group 1. Also note, we specified Maximum Likelihood Estimation as the Factor Method (`fm = "mle"`) because this is the method used by default with the 'factanal' (i.e. factor analysis) function of the 'stats' package. We specified the number of observations (i.e. number of rows, cases, or participants) using the length of the group 1 vector (`g1`). Recall from above, the group 1 vector contains the row numbers of all the participants from group 1.

```
R Console (64-bit)
File Edit Misc Packages Windows Help
> vss(x = vss.df[g1,6:35], n = 3, rotate = "oblimin",
+     fm = "mle", n.obs = length(g1))

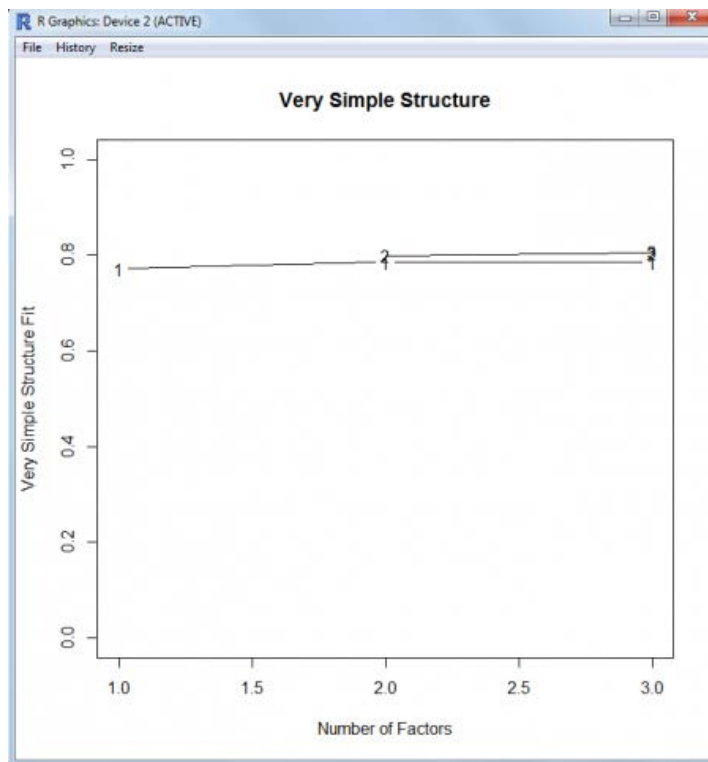
Very Simple Structure
Call: vss(x = vss.df[g1, 6:35], n = 3, rotate = "oblimin", fm = "mle",
n.obs = length(g1))
VSS complexity 1 achieves a maximum of 0.79 with 2 factors
VSS complexity 2 achieves a maximum of 0.8 with 3 factors

The Velicer MAP achieves a minimum of 0 with 2 factors
BIC achieves a minimum of -1900.78 with 2 factors
Sample Size adjusted BIC achieves a minimum of -707.63 with 2 factors

Statistics by number of factors
  vss1 vss2  map dof chisq  prob sqresid fit RMSEA  BIC SABIC complex eChisq SRMR eCRMS
1 0.77 0.0 0.0503 405 2434 7.3e-286 32 0.77 0.1115 -10 1275 1.0 7303 0.142 0.147
2 0.79 0.8 0.0049 376 369 6.0e-01 28 0.80 0.0048 -1901 -708 1.0 224 0.025 0.027
3 0.78 0.8 0.0064 348 328 7.7e-01 27 0.81 0.0000 -1773 -668 1.1 186 0.023 0.025

eBIC
1 4858
2 -2046
3 -1914
> |
```

The first few rows of output (i.e. "Very Simple Structure" table) show the function called and the *maximum* complexity values. This is a good example because the VSS complexity rows are conflicting; VSS complexity 1 shows a 2-factor model is best while VSS complexity 2 indicates a 3-factor model is best. The VSS complexity 2 is a bit misleading because both the 2-factor model and 3-factor model display a VSS complexity 2 of 0.80; as can be seen in the first column of output under the "Statistics by number of factors" table. So, in fact both complexity 1 and complexity 2 are in agreement. Furthermore, the Velicer MAP *minimum* is reached with the 2-factor model; which can also be seen in the third column of the "Statistics by number of factors" table. The Bayesian Information Criterion (BIC) *minimum* is reached with the 2-factor model; as well as the Sample Size adjusted BIC (SABIC) – shown in columns 10 and 11 respectively of the "Statistics by number of factors" table. The 'vss' function also produces a plot (by default) which shows the number of factors on the x-axis and the VSS (complexity) Fit along the y-axis with lines and numbers in the Cartesian plane representing the (3) different factor models (see below).



To interpret the graph, focus on the model (1, 2, or 3 factor models) which has the highest line (and numerals) in relation to the y-axis; but also note any transitions of the model lines. In this example, the transitions are all very nearly flat but a later example will better demonstrate the utility of this type of plot.

Next, we can verify the fit of our 2-factor model using either the 'fa' function (from the 'psych' package) and / or the 'factanal' function (of the 'stats' package).

```

R Console (64-bit)
File Edit Misc Packages Windows Help
> fa(r = vss.df[g1,6:35], nfactors = 2, rotate = "oblimin", fm = "mle")
Factor Analysis using method = ml
Call: fa(r = vss.df[g1, 6:35], nfactors = 2, rotate = "oblimin", fm = "mle")
Standardized loadings (pattern matrix) based upon correlation matrix
      ML1  ML2  h2  u2  com
11  0.89  0.03  0.82  0.18  1.0
12  0.32 -0.04  0.65  0.35  1.0
13  0.83 -0.01  0.68  0.32  1.0
14  0.49 -0.01  0.23  0.77  1.0
15  0.72 -0.01  0.51  0.49  1.0
16  0.65  0.01  0.43  0.57  1.0
17  0.65  0.00  0.43  0.57  1.0
18  0.48  0.12  0.29  0.71  1.1
19  0.65  0.00  0.42  0.58  1.0
110 0.66  0.03  0.45  0.55  1.0
111 0.80  0.03  0.66  0.34  1.0
112 0.53 -0.01  0.28  0.72  1.0
113 0.82  0.01  0.39  0.61  1.0
114 0.69 -0.03  0.46  0.54  1.0
115 0.84 -0.02  0.69  0.31  1.0
116 -0.01  0.90  0.80  0.20  1.0
117 0.04  0.74  0.58  0.42  1.0
118 -0.01  0.79  0.62  0.38  1.0
119 -0.03  0.52  0.26  0.74  1.0
120 0.02  0.65  0.44  0.56  1.0
121 -0.03  0.58  0.33  0.67  1.0
122 0.02  0.55  0.31  0.69  1.0
123 0.01  0.39  0.16  0.84  1.0
124 0.00  0.67  0.45  0.55  1.0
125 -0.06  0.70  0.46  0.54  1.0
126 0.04  0.76  0.61  0.39  1.0
127 0.11  0.38  0.20  0.80  1.2
128 0.07  0.54  0.33  0.67  1.0
129 -0.04  0.68  0.44  0.56  1.0
130 0.01  0.80  0.65  0.35  1.0

      SS loadings      ML1 ML2
Proportion Var      7.39 6.60
Cumulative Var      0.25 0.22
Proportion Explained 0.53 0.47
Cumulative Proportion 0.53 1.00

With factor correlations of
      ML1 ML2
ML1 1.00 0.44
ML2 0.44 1.00

Mean item complexity = 1
Test of the hypothesis that 2 factors are sufficient.

The degrees of freedom for the null model are 435 and the objective function was 16.06 with Chi$
The degrees of freedom for the model are 376 and the objective function was 0.91

```

*Note: the last few lines of output from the 'fa' function are cut off (i.e. not shown).

```

R Console (64-bit)
File Edit Misc Packages Windows Help
> factanal(vss.df[g1,6:35], factors = 2, rotation = "oblimin")
Call:
factanal(x = vss.df[g1, 6:35], factors = 2, rotation = "oblimin")
Uniquenesses:
  i1  i2  i3  i4  i5  i6  i7  i8  i9  i10  i11  i12  i13  i14  i15  i16
0.178 0.351 0.325 0.768 0.492 0.574 0.573 0.706 0.580 0.547 0.337 0.723 0.608 0.542 0.313 0.200
117 118 119 120 121 122 123 124 125 126 127 128 129 130
0.422 0.379 0.742 0.565 0.675 0.694 0.841 0.554 0.545 0.390 0.804 0.665 0.558 0.355

Loadings:
      Factor1 Factor2
11  0.891
12  0.823
13  0.828
14  0.487
15  0.717
16  0.647
17  0.653
18  0.478  0.123
19  0.647
110 0.660
111 0.801
112 0.530
113 0.821
114 0.688
115 0.838
116  0.899
117  0.744
118  0.793
119  0.521
120  0.649
121  0.584
122  0.547
123  0.394
124  0.669
125  0.700
126  0.762
127 0.110 0.384
128  0.542
129  0.680
130  0.799

      SS loadings      Factor1 Factor2
Proportion Var      0.245  0.219
Cumulative Var      0.245  0.464

Factor Correlations:
      Factor1 Factor2
Factor1  1.000 -0.435
Factor2 -0.435  1.000

```

*Note: last few lines of output from the 'factanal' function are cut off (i.e. not shown).

We will now assess the group 2 (g2) data. This group is believed to be best served with a 3-factor model; so we specify 4 factors ($n = 4$) in the 'vss' function call; again with the factor method set to Maximum Likelihood Estimation ($fm = "mle"$) and an oblique rotation strategy ($rotate = "oblimin"$).

```

R Console (64-bit)
File Edit Misc Packages Windows Help
> vss(x = vss.df[g2,6:35], n = 4, rotate = "oblimin",
+   fm = "mle", n.obs = length(g2))

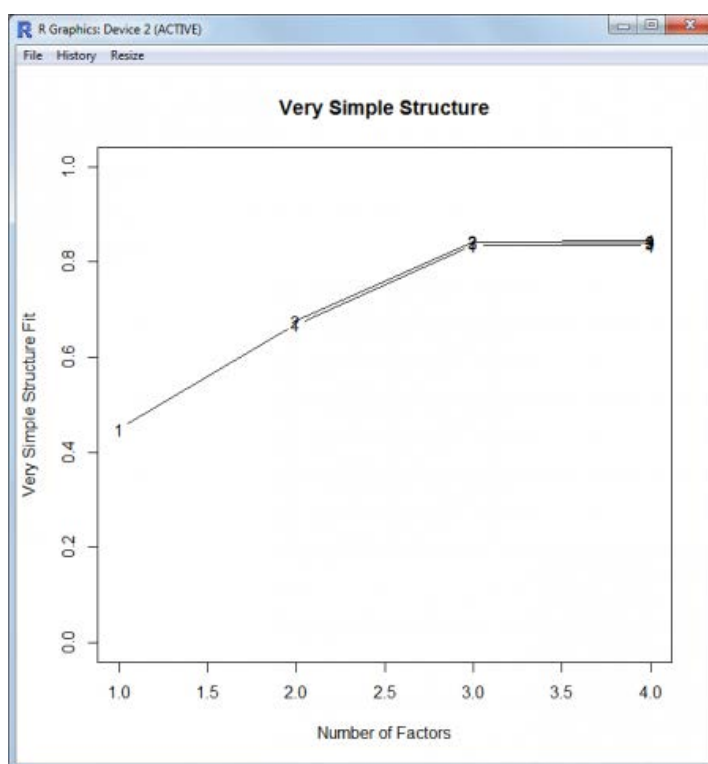
Very Simple Structure
Call: vss(x = vss.df[g2, 6:35], n = 4, rotate = "oblimin", fm = "mle",
  n.obs = length(g2))
VSS complexity 1 achieves a maximum of 0.84 with 3 factors
VSS complexity 2 achieves a maximum of 0.84 with 3 factors

The Velicer MAP achieves a minimum of 0 with 3 factors
BIC achieves a minimum of -2059.87 with 3 factors
Sample Size adjusted BIC achieves a minimum of -954.62 with 3 factors

Statistics by number of factors
  vss1 vss2  map dof  chisq prob  sqresid  fit RMSEA  BIC  SABIC  complex  eChisq  SRMR  eCRMS  eBIC
1  0.45  0.00  0.0587 405  8098 0.00    54  0.45  0.140  5308  6594    1  32395  0.195  0.202  29604
2  0.67  0.68  0.0365 376  3757 0.00    32  0.68  0.096  1167  2361    1  13427  0.125  0.135  10837
3  0.84  0.84  0.0049 348   338 0.64    16  0.84  0.000  -2060  -955    1   195  0.015  0.017  -2203
4  0.84  0.84  0.0065 321   301 0.79    15  0.85  0.000  -1911  -891    1   174  0.014  0.017  -2038
> |

```

In this example all of the indices in the top table ("Very Simple Structure") are in agreement; although both VSS complexity metrics display the same *maximum* for a 3-factor model and a 4-factor model. Looking at the first two columns of the "Statistics by number of factors" table shows the identical complexity *maximums* (0.84) for both the 3-factor model (row 3) and the 4-factor model (row 4) with both complexities 1 and 2 (columns 1 and 2). But, given the other indices agreement in support of the 3-factor model, that would be the model most appropriate. The plot (below) reinforces the interpretation of the tabular output above.



The plot (above) shows that the 3-factor model is meaningfully better than the 1-factor or 2-factor models and the 4-factor model does not show any improvement over the 3-factor model – which is evident because the number 4 in the plot is not [further] above the line associated with the 3-factor model (i.e. no gain or transition upward; as is the case from 1-factor to 2-factors and to 3-factors). Therefore, we fit the 3-factor model to our data using the 'fa' function (of the 'psych' package) and / or the 'factanal' function of the 'stats' package.

```

R Console (64-bit)
File Edit Misc Packages Windows Help
> fa(r = vss.df[g2,6:35], nfactores = 3, rotate = "oblimin", fm = "ml")
Factor Analysis using method = ml
Call: fa(r = vss.df[g2, 6:35], nfactores = 3, rotate = "oblimin", fm = "ml")
Standardized loadings (pattern matrix) based upon correlation matrix
      ML2  ML1  ML3  s2  u2  com
i1 -0.01  0.90  0.00  0.80  0.20  1
i2 -0.02  0.83  0.01  0.69  0.31  1
i3  0.04  0.78  0.01  0.63  0.37  1
i4  0.00  0.46  0.01  0.22  0.78  1
i5  0.03  0.68  0.00  0.47  0.53  1
i6  0.00  0.62  0.02  0.39  0.61  1
i7  0.00  0.59  -0.03  0.34  0.66  1
i8  0.01  0.46  0.02  0.22  0.78  1
i9  0.01  0.71  -0.01  0.50  0.50  1
i10 -0.04  0.69  0.00  0.46  0.54  1
i11  0.77  -0.03  0.03  0.59  0.41  1
i12  0.50  0.06  -0.03  0.26  0.74  1
i13  0.64  -0.01  -0.01  0.40  0.60  1
i14  0.72  0.01  0.02  0.53  0.47  1
i15  0.80  0.03  -0.01  0.44  0.36  1
i16  0.90  -0.01  -0.01  0.80  0.20  1
i17  0.79  0.00  -0.01  0.62  0.38  1
i18  0.79  0.02  0.01  0.64  0.36  1
i19  0.49  -0.06  -0.01  0.23  0.77  1
i20  0.47  -0.02  0.00  0.45  0.55  1
i21  0.04  0.00  0.69  0.37  0.63  1
i22  0.04  0.01  0.58  0.35  0.65  1
i23  0.02  0.04  0.52  0.29  0.71  1
i24 -0.01  0.00  0.71  0.50  0.50  1
i25 -0.01  -0.01  0.71  0.50  0.50  1
i26 -0.01  0.01  0.81  0.66  0.34  1
i27 -0.03  0.04  0.49  0.24  0.76  1
i28  0.02  0.02  0.64  0.42  0.58  1
i29  0.00  -0.02  0.72  0.51  0.49  1
i30 -0.02  -0.01  0.80  0.63  0.37  1

      ML2  ML1  ML3
SS loadings  5.17  4.72  4.45
Proportion Var  0.17  0.16  0.15
Cumulative Var  0.17  0.33  0.48
Proportion Explained  0.36  0.39  0.31
Cumulative Proportion  0.36  0.69  1.00

With factor correlations of
      ML2  ML1  ML3
ML2  1.00  0.25  0.12
ML1  0.25  1.00  0.25
ML3  0.12  0.25  1.00

Mean item complexity = 1
Test of the hypothesis that 3 factors are sufficient.
The degrees of freedom for the null model are 435 and the objective function was 14.12 with ChiS

```

*Note: the last few lines of output from the 'fa' function are cut off (i.e. not shown).

```

R Console (64-bit)
File Edit Misc Packages Windows Help
> factanal(vss.df[g2,6:35], factors = 3, rotation = "oblimin")
Call:
factanal(x = vss.df[g2, 6:35], factors = 3, rotation = "oblimin")
Uniquenesses:
  i1  i2  i3  i4  i5  i6  i7  i8  i9  i10  i11  i12  i13  i14  i15  i16
0.197 0.311 0.368 0.764 0.531 0.612 0.669 0.780 0.502 0.542 0.407 0.739 0.599 0.467 0.355 0.203
  i17  i18  i19  i20  i21  i22  i23  i24  i25  i26  i27  i28  i29  i30
0.378 0.365 0.774 0.553 0.631 0.651 0.713 0.504 0.504 0.338 0.756 0.584 0.485 0.365

Loadings:
      Factor1 Factor2 Factor3
i1      0.898
i2      0.833
i3      0.782
i4      0.469
i5      0.678
i6      0.618
i7      0.588
i8      0.462
i9      0.705
i10     0.687
i11     0.773
i12     0.497
i13     0.637
i14     0.725
i15     0.796
i16     0.896
i17     0.750
i18     0.791
i19     0.487
i20     0.673
i21      0.601
i22      0.582
i23      0.520
i24      0.706
i25      0.709
i26      0.813
i27      0.485
i28      0.638
i29      0.722
i30      0.802

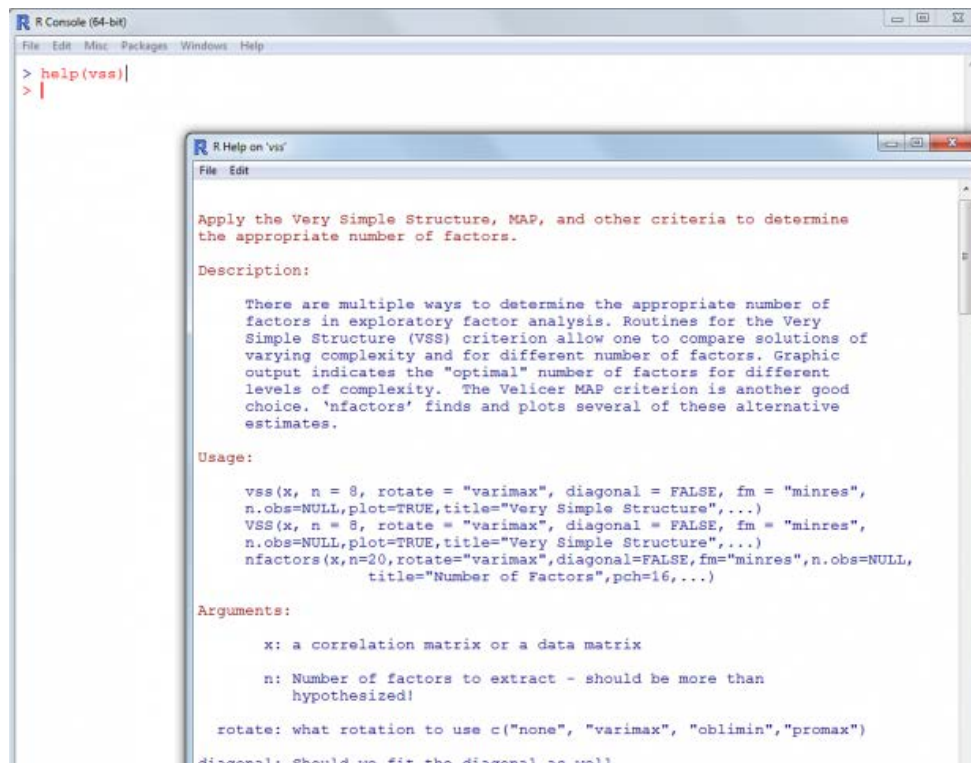
      Factor1 Factor2 Factor3
SS loadings  5.183  4.711  4.442
Proportion Var  0.172  0.157  0.148
Cumulative Var  0.172  0.329  0.477

Factor Correlations:
      Factor1 Factor2 Factor3
Factor1  1.000  0.246  -0.252
Factor2  0.246  1.000  -0.119

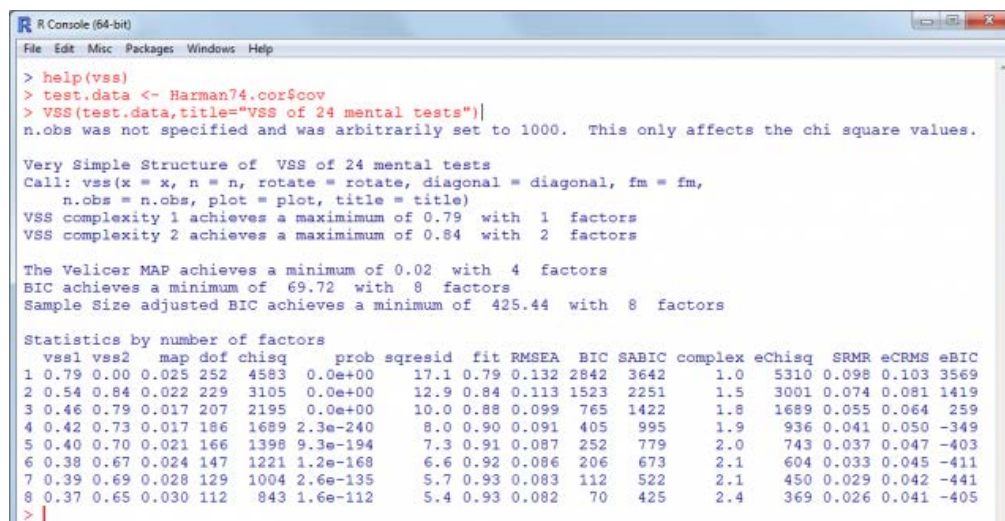
```

*Note: last few lines of output from the 'factanal' function are cut off (i.e. not shown).

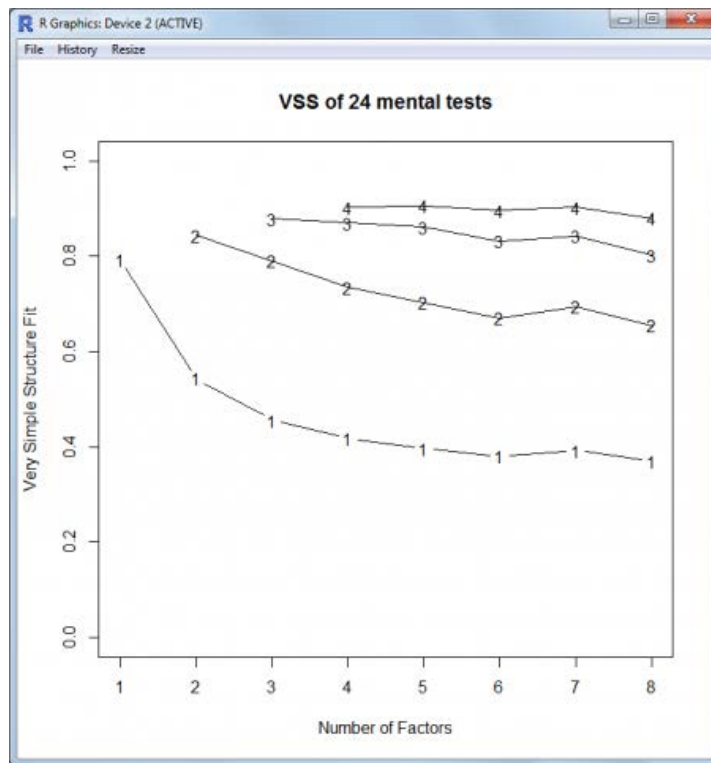
The next example is straight from the help file of the 'vss' function and is discussed here because it demonstrates a situation when the tables of output from the 'vss' function are not in agreement. When this situation occurs, one must rely upon the plot produced by the 'vss' function rather than the textual output. First, open the help file (here the plain text version is shown).



Next, scroll to the bottom of the help file and copy / paste the relevant lines of script into the R console.



As mentioned previously, the tables of statistics do not provide a clear answer to the question of which factor model is best (i.e. how many factors should be extracted). However, if we review the associated plot, we can clearly see the 4-factor model is the best (i.e. highest; even when embedded within models with more than 4 factors, with good separation from previous models).



Conclusions

The intent of this article was to raise awareness of the dangers of using only one criteria or method for deciding upon the number of factors to extract when conducting factor analysis. This article also demonstrated the ease with which an analyst can compute and evaluate several such criteria to reach a more informed decision. More extensive examples of the data analysis solutions are available at the RSS [Do-it-yourself Introduction to R](#) course page. Lastly, a copy of the script file used for the above examples is available [here](#).

Until next time; remember what George Carlin said: "just 'cause you got the monkey off your back doesn't mean the circus left town."

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